

The discretization

- The icosahedron couples to its dual dodecahedron (i.e.

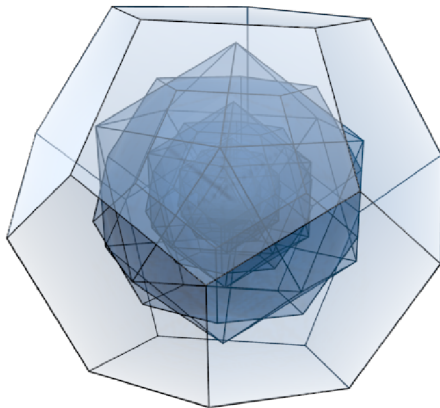
$$k^d = k \Rightarrow k^i = \sqrt{\varphi \frac{\sqrt{5}}{3} k}.$$

Where $\varphi = (1 + \sqrt{5})/2$ is the golden ratio

- The triad condition $\mathbf{k} + \mathbf{p} + \mathbf{q} = 0$, can now be satisfied with:

$$k_n \hat{\mathbf{k}}_\ell^i + k_{n-1} \hat{\mathbf{k}}_{\ell'}^d + k_{n+1} \hat{\mathbf{k}}_{\ell''}^d = 0$$

$$k_n \hat{\mathbf{k}}_\ell^d + k_{n-1} \hat{\mathbf{k}}_{\ell'}^i + k_{n+1} \hat{\mathbf{k}}_{\ell''}^i = 0$$



What we solve?

- At each node (i.e. vertex ℓ of shell n), we need to solve, the Navier-Stokes equation in spectral form:

$$\partial_t u_{n,\ell}^i + i k_{n\ell}^\kappa \left[\delta_{ij} - \frac{k_{n\ell}^i k_{n\ell}^j}{k_n^2} \right] \sum_{n',\ell'} u_{n',\ell'}^{*\kappa} u_{n'',\ell''}^{j*} = 0$$

- We can “flatten” using $m = \text{floor}(n/2) \times 32 + (n \bmod 2) \times N_{fs} + \ell$ (and then $m \rightarrow n$), where N_{fs} is the number of vertices of the first shell.
- This gives a network model, where each “node” is connected to a “pair”.

