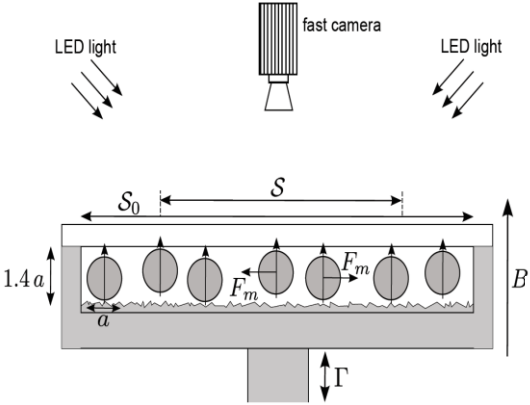


# “Granular turbulence” in a driven system of magnetized particles

Michael Berhanu<sup>1</sup>, Simon Merminod<sup>2</sup>, Gustavo Castillo<sup>3</sup> & Eric Falcon<sup>1</sup>

<sup>1</sup> MSC, Université de Paris, France, <sup>2</sup> Harvard University, MA, USA, <sup>3</sup> Universidad O'Higgins, Rancagua, Chile



Kinetic energy per particle

$$E_c = \frac{1}{2} m \langle v_x^2 + v_y^2 \rangle$$

Potential energy per particle

$$E_m = \frac{1}{N} \sum_{i=1}^N \sum_{j=i+1}^N U_{m,ij}$$

$$\varepsilon = \frac{E_m}{E_c} \propto \frac{B^2}{\langle \|\mathbf{v}_{rms}\|^2 \rangle}$$

Acceleration rms  $\Gamma=1.6$  g

$0 < B < 430$  G

2D velocities  
from particle tracking

$U_{m,\langle ij \rangle}$  dipolar potential  
energy of a pair  $ij$

$$U_{m,\langle ij \rangle} = -\frac{\pi}{16\mu_0} B^2 \frac{a^6}{r_{ij}^3}$$

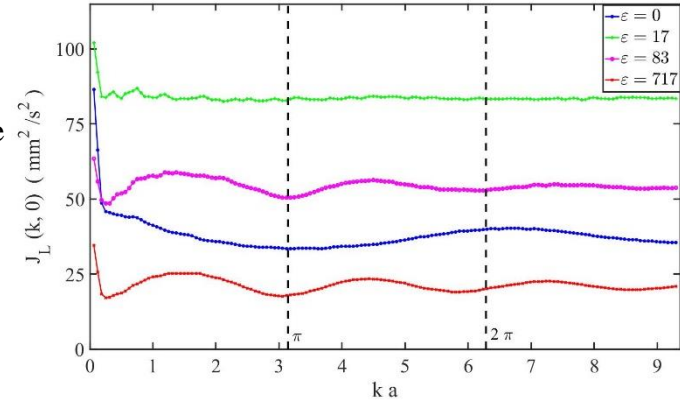
Competition between remote  
interactions vs agitation

Velocity fluctuations. Longitudinal current correlations in spatial Fourier space

$$J_l(\mathbf{k}, t) = \left\langle \frac{1}{N} \sum_{i,j=1}^N (\hat{\mathbf{k}} \cdot \mathbf{v}_i(t)) (\hat{\mathbf{k}} \cdot \mathbf{v}_j(0)) e^{i\mathbf{k} \cdot (\mathbf{r}_i(t) - \mathbf{r}_j(0))} \right\rangle$$

$$J_l(k, t) = (2\pi)^{-1} \int_0^{2\pi} J_l(\mathbf{k}, t) d\theta \quad \text{Isotropic average}$$

Kinetic longitudinal energy spectrum.  
For  $\varepsilon=17$ , flat spectrum. **Equipartition.**

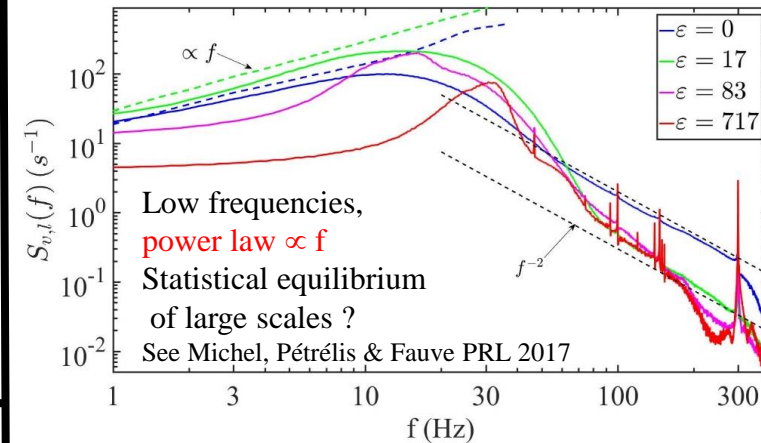


• Space-time spectrum  
of longitudinal kinetic energy

$$S_{v,l}(k, \omega) = \text{Re} \int_0^\infty \int_0^{2\pi} J_l(\mathbf{k}, t) k d\theta e^{i\omega t} dt$$

• Deducing the **time spectrum** from the space spectrum  
from the experimental dispersion relation

$$S_{v,l}(f) = 2\pi / (\partial\omega_{R,l} / \partial k) k_R(f) S_{v,l}(k)$$



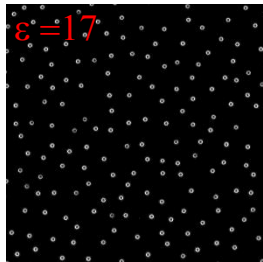
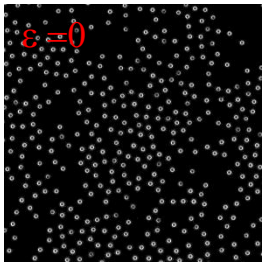
• Large frequencies and low  $\varepsilon$ : power law  $\propto f^2$ , to investigate  
maybe related to the life time of excitations.

• Analogy with dissipative turbulence in active matter

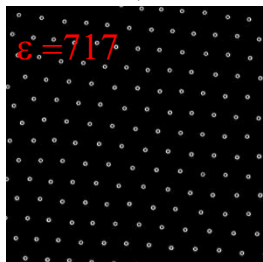
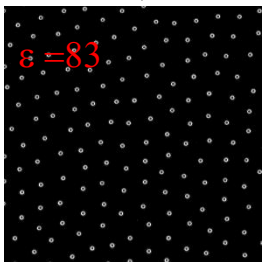
See R. Alert, J.F. Joanny and J. Casademunt Nat. Phys.2020

Different regimes as a function of  $\varepsilon$ :

**Granular gas** ( $0 \leq \varepsilon < 10.7$ ) **Dipole fluid** ( $10.7 < \varepsilon < 21.9$ )



**Partial order** ( $21.9 < \varepsilon < 185$ ) **Crystal** ( $185 < \varepsilon < 1484$ )

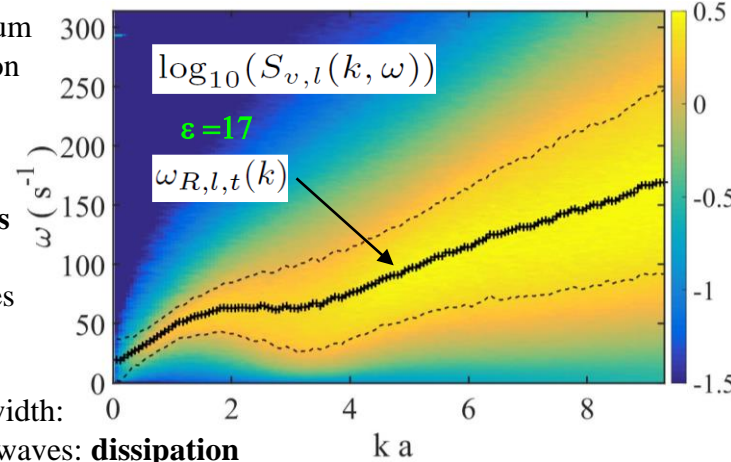


Maxima of spectrum  
defines a dispersion  
relation  $\omega_R(\mathbf{k})$

Propagation of  
**mechanical waves**  
analog to  
compression waves  
in fluids.

Significant R.D. width:

small life time of waves: **dissipation**



• Random dispersive waves + Nonlinear potential:  
ingredients of wave turbulence: “granular” turbulence?

• Homogeneous forcing in  $k$ -space, filtered by the wave dynamics.  
No well defined scale for energy injection.