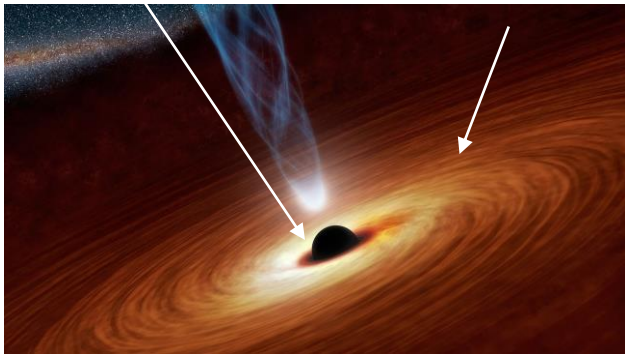


# Angular momentum transport by turbulence in Keplerian flows

**M. Vernet, S. Fauve & C. Gissinger**  
Laboratoire de Physique de l'ENS, Paris  
*marlone.vernet@phys.ens.fr*

Black hole

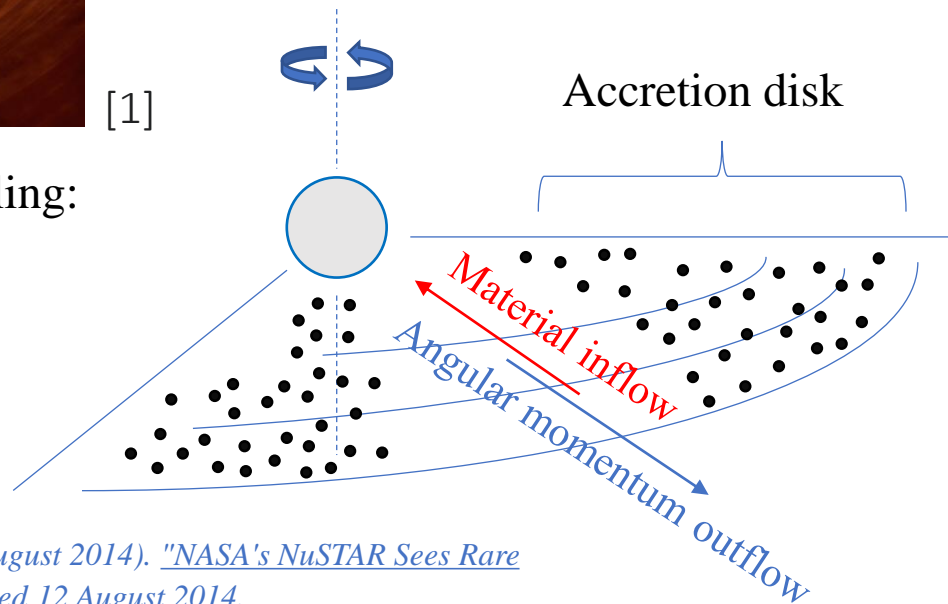
Accretion disk



Massive central body

[1]

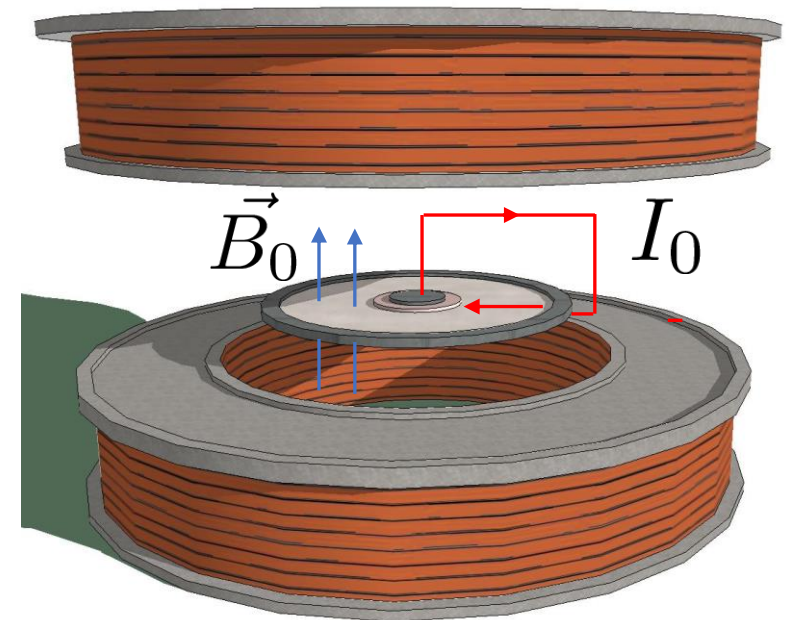
Accretion disk



Keplerian rotation rate scaling:

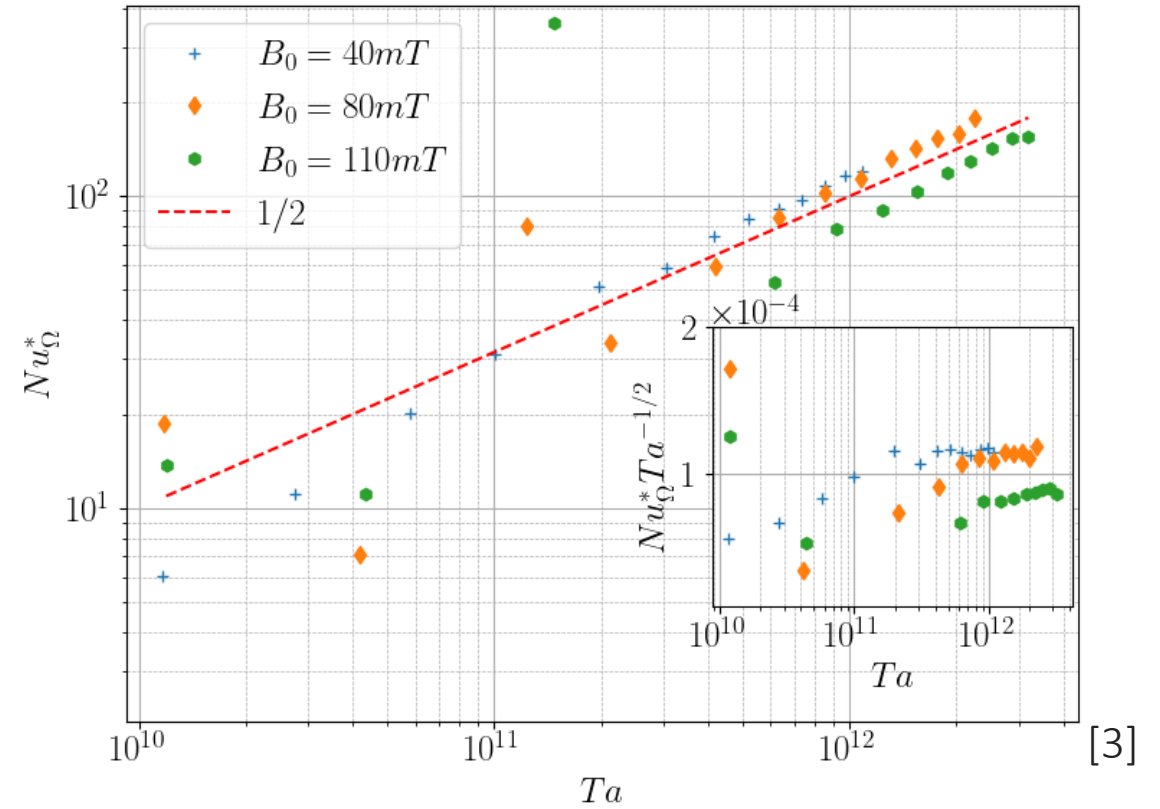
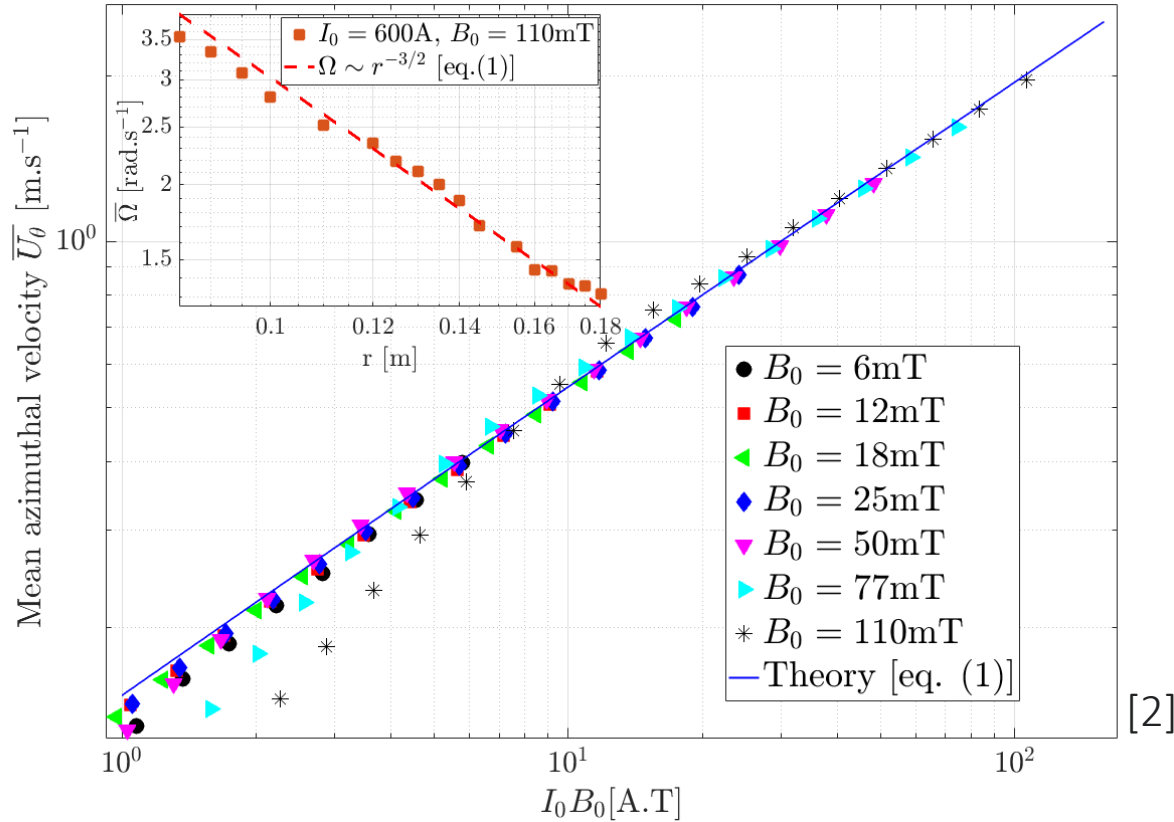
$$\Omega \propto \frac{1}{r^{3/2}}$$

Kepler experiment :



[1] Clavin, Whitney; Harrington, J.D. (12 August 2014). "NASA's NuSTAR Sees Rare Blurring of Black Hole Light". NASA. Retrieved 12 August 2014.

# Kraichnan's ultimate regime :



Flux of angular velocity :

$$\overline{J}_\Omega^* = r^3 (\overline{u_r^* \Omega^*} - \nu \partial_r (\overline{\Omega}))$$

Kraichnan's regime :

$$J_{lam} = 2\nu r \overline{u_\theta}$$

Nusselt number :  $Nu_\Omega^* = \frac{\overline{J}_\Omega^*}{J_{lam}}$

$$Nu_\Omega^* \propto \sqrt{Ta}$$

- Fully turbulent state
- Keplerian rotation flow

$$\overline{u_\theta} = \frac{\log Re}{\kappa} \sqrt{\frac{I_0 B_0}{4\pi \rho r}}$$

- Kepler experiment therefore gives predictions for accretion rates, which enables direct comparisons with astrophysical objects.

[2] Vernet, M., Pereira, M., Fauve, S., & Gissinger, C. (2021). Turbulence in electromagnetically driven Keplerian flows. *Journal of Fluid Mechanics*, 924, A29.

[3] Vernet et al. Submitted PRL.